

# Return Levels of Warm Monthly Temperature Extremes based on CMIP5 Multi-Model Simulations

L. Cheng, T. J. Phillips, A. AghaKouchak

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# Non-stationary Return Levels of CMIP5 Multi-Model

- Temperature Extremes
- Linyin Cheng · Thomas J. Phillips

Amir AghaKouchak

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Linyin Cheng University of California Irvine, E4130 Engineering Gateway Irvine, CA 92697-2175, USA

University of California Irvine, E4130 Engineering Gateway Irvine, CA 92697-2175, USA (Corresponding Author, E-mail: amir.a@uci.edu)

Thomas J. Phillips

Lawrence Livermore National Laboratory, 7000 East Avenue Livermore, CA 94550, USA

**Abstract** The objective of this study is to evaluate to what extent the CMIP5 climate model simulations of the climate of the  $20^{th}$  century can represent observed warm monthly temperature extremes under a changing environment. The biases and spatial patterns of 2-, 10-, 25-, 50- and 100-year return levels of the annual maxima of monthly mean temper-11 ature (hereafter, annual temperature maxima) from CMIP5 simulations 12 are compared with those of Climatic Research Unit (CRU) observational 13 data considered under a non-stationary assumption. The results show that 14 CMIP5 climate models collectively underestimate the mean annual max-15 ima over arid and semi-arid regions that are most subject to severe heat 16 waves and droughts. Furthermore, the results indicate that most climate models tend to underestimate the historical annual temperature maxima over the United States and Greenland, while generally disagreeing in their simulations over cold regions. Return level analysis shows that with respect to the spatial patterns of the annual temperature maxima, there are 21 good agreements between the CRU observations and most CMIP5 sim-22 ulations. However, the magnitudes of the simulated annual temperature 23 maxima differ substantially across individual models. Discrepancies are generally larger over higher latitudes and cold regions.

- **Keywords** Temperature · Climate · CMIP5 · Extremes · Return Level ·
- 27 Non-stationary

#### 8 1 Introduction

year were killed in the United States by excessive heat (NOAA (1995); Kilbourne (1997)). In fact, in this period over the United States, exces-31 sive heat accounted for more reported deaths annually than hurricanes, floods, tornadoes, and lightning combined (NOAA (1995)). Furthermore, agriculture products such as wheat, rice, corn and maize can be significantly reduced by extreme high temperatures at key development stages (NOAA (1980); Hoerling (2013)). High temperatures also affect irrigation and evaporation (Sorooshian et al. (2014)), drought development (Aghakouchak et al. (2014)), energy production and consumption (Tarroja et al. (2014b)) as well as greenhouse gas emissions associated with energy production (Tarroja et al. (2014a)). Numerous studies indicate that temperature extremes are likely to intensify in the future under different plausible climate scenarios (Alexander et al. (2006); IPCC (2007)). Climate model simulations have been widely used to study extreme weather and climate across different spatial and temporal scales. Recently, international climate modeling groups have provided Coupled Model Intercomparison Project Phase 5 (CMIP5) historical and projected climate simulations (Taylor et al. (2012)). The scope of CMIP5 also is broader 47 than previous model intercomparison projects (e.g. CMIP3), with carbon emission-driven Earth System Model (ESM) experiments now represented along with the typical concentration-driven atmosphere-ocean general circulation model (AOGCM) simulations (Meehl and Bony (2011)). Thus, 51 the multi-model gridded CMIP5 datasets provide an unprecedented opportunity to analyze and assess climate variability and change. However, model simulations are known to have high uncertainty (Kharin et al. (2013); Mehran et al. (2014); Liu et al. (2014); Sillmann et al. (2013)), and

During the period 1979 - 1992, on average nearly four hundred people each

different methods have been develop to assess their consistency against observations (Gleckler et al. (2008); AghaKouchak and Mehran (2013); Phillips and Gleckler (2006)).

In a recent study, Kharin et al. (2013) argued that the global warm 59 temperature extremes in the late  $20^{th}$  century climate are reasonably simulated by the CMIP5 models (differences in CMIP5 models and reanalysis 61 data were within a few degrees <sup>o</sup>C over most of the globe). Furthermore, the study showed that the spread amongst CMIP5 models for several temperature indices defined by the Expert Team on Climate Change Detection and Indices (ETCCDI; Zhang and Zwiers (2013)) is reduced compared to CMIP3 models (see also Sillmann et al. (2013)). However, 66 the inter-model differences of warm temperature extremes are generally 67 large over land with a standard deviation of around 4 °C (Kharin et al. (2013)). Kharin et al. (2013) concluded that upward trends of warm extremes exceed those of cold extremes over tropical and subtropical land regions. Morak et al. (2013) showed that there is a significant increase in the trend in warm temperature extremes during both boreal cold and 72 warm seasons over the second half of the 20th century. Using CMIP5 simulations and observations, Hao et al. (2013) demonstrated that concurrent warm/dry and warm/wet extremes have increased substantially in the second half of the  $20^{th}$  century.

Return periods and return levels (also known as return values) are often used to describe and assess risk of extremes (Cooley et al. (2007); AghaKouchak and Nasrollahi (2010); Katz (2010); Cooley (2013)). In theory, the return period (T) of an event is the inverse of its probability of occurrence in any given year. That is, the n-year return level corresponds to an exceedance probability (by an annual extreme) of 1/n. In the statistical literature, there are different definitions for return period and return

level; for alternative definitions, the interested reader is referred to Bonnin et al. (2004), Mays (2010), and AghaKouchak et al. (2013).

In recent years, Extreme Value Theory (EVT) has been widely used for 86 analysis of climate extremes and their return levels (Zwiers and Kharin 87 (1998); Clarke (2002); Katz et al. (2002); Kharin and Zwiers (2005); Parey et al. (2010); Kunkel (2013); Cheng et al. (2014b); Cooley (2013)). Fisher and Tippett (1928) introduced the concept of asymptotic theory in extreme value distributions and laid the foundation for a generalized approach to extreme value analysis. Gnedenko (1943) mathematically proved that three families of extreme value distributions - namely Weibull, Gumbel and Fréchet - can represent the limiting distributions 94 of extremes in random variables. The Generalized Extreme Value (GEV) distribution is essentially a combination of these three distribution families, and has been applied in a variety of studies (Gumbel (1942); Smith (2001); Katz (2013)).

Numerous studies indicate that climatic extremes (e.g., hot days, heavy precipitation) have increased significantly, particularly in the second half 100 of the  $20^{th}$  century (Karl and Knight (1998); Easterling et al. (2000); 101 Vose et al. (2005); Hansen et al. (2010); Villarini et al. (2011); Hao et al. 102 (2013); Field et al. (2012); Wehner (2013)). In addition to their num-103 ber, the frequency of extremes has changed in the past, and is likely to 104 change in the future (Milly et al. (2008); Easterling et al. (2000); IPCC 105 (2007)). It is evident that ignoring time-varying (non-stationary) behavior 106 of extremes could lead to underestimation of extremes and considerable damage to human life and society (McMichael (2003); Cheng and AghaKouchak (2014)). Therefore, it is necessary to assess non-stationarity in the CMIP5 climate models simulations, and to document the extent to which 110 the model-simulated patterns are consistent with observations. 111

In most previous climate model evaluation studies, the first or second 112 order statistics of models are compared against observations. The primary 113 objective of this paper is to evaluate to what extent the CMIP5 model simulations of the historical climate of the period 1901-2005 can represent 115 observed warm monthly temperature extremes under the non-stationary 116 assumption. In this study, the GEV distribution is used to investigate 117 the return levels of annual monthly temperature maxima considering a 118 changing climate. The return levels of temperature maxima estimated 119 from the CMIP5 climate simulations are compared with those of Climatic 120 Research Unit (CRU) temperature observations. 121

The remainder of the paper is organized as follows. In section 2, the data sets and study area are discussed. Section 3 presents the methodology for non-stationary extreme value analysis. The results including representation of annual maxima in their return levels are provided in Section 4. Section 5 summarizes the main results and offers concluding remarks.

### 2 Study Area and Data Resources

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Monthly observations of temperature provided by the Climatic Research 129 Unit (CRU, New et al. (2000); Mitchell and Jones (2005)), available in 130 a  $0.5^{\circ}$  spatial resolution, are used as reference data. In this study, 41 131 CMIP5 historical monthly temperature simulations from 1901 to 2005 132 are subjected to extreme value analysis, and a subset of 17 of these sim-133 ulations are investigated in more detail. These data sets represent the 134 most extensive and ambitious multi-model simulations that contribute to the World Climate Research Programme's CMIP multi-model dataset (Meehl and Bony (2011); Taylor et al. (2012)). For this extreme value 137 analysis, the CMIP5 model simulations and CRU observations all are re-

gridded to a common  $2 \times 2$ -degree resolution. This regridding entailed use 139 of bilinear interpolation, with special attention given to appropriate use of model-specific land fraction masks so as to minimize data distortions along coastlines. The selected models (Table 1) include physical climate 142 models (without a prognostic global carbon cycle), as well as earth sys-143 tem models (with the designation "ESM" appearing in the model title). 144 The former are run in a standard "historical climate" configuration with 145 prescribed historically increasing CO<sub>2</sub> concentrations and the latter are 146 run with CO<sub>2</sub> emissions (fluxes corresponding to the prescribed histori-147 cally increasing CO<sub>2</sub> concentrations–designated as "\_esm" experiments in Table 1).

This study focuses on global land areas (excluding Antarctica) for 150 which the CRU observations are provided. From CRU observations and 151 CMIP5 simulations, pixel-based annual monthly temperature maxima 152 (hereafter, annual temperature maxima) are extracted for estimation of 153 extreme temperature return levels. It should be noted that the Hadley Centre has adopted an unconventional time model for all their CMIP5 155 output data, with an endpoint in November rather than December of 156 2005, and thus the HadGEM2 outputs include one month fewer data 157 than those of the other models. This issue will not affect the results in 158 the Northern Hemisphere since the annual maxima of monthly data do 159 not often occur in December. However, it might slightly impact the anal-160 yses in the Southern Hemisphere. 161

## 162 3 Methodology

The cumulative distribution function (CDF) of the GEV can be written as (Coles (2001)):

$$\Psi(x) = exp\left\{-\left(1 + \xi\left(\frac{x - \mu}{\sigma}\right)\right)^{\frac{-1}{\xi}}\right\} \qquad (1 + \xi\left(\frac{x - \mu}{\sigma}\right) > 0) \quad (1)$$

where  $\Psi(x)$  refers to the limiting CDF of the block maxima of inde-165 pendently and identically distributed random variables (Leadbetter et al. (1983)). To avoid serial dependence in the data, in this study, only one value per year (annual maxima) is sampled for extreme value analysis. The GEV distribution models different characteristics of extremes us-169 ing three parameters  $\theta = (\mu, \sigma, \xi)$ : location parameter  $(\mu)$ , scale parameter 170  $(\sigma)$ , and shape parameter  $(\xi)$ . The location parameter indicates where the extremes distribution is centered, whereas the scale parameter specifies the deviations around  $\mu$ . The shape parameter describes the tail behavior 173 of the GEV distribution such that  $\xi = 0$ ,  $\xi < 0$  and  $\xi > 0$  represent the 174 Gumbel, Weibull and Fréchet families, respectively (Coles (2001)). The 175 GEV CDF  $(\Psi(x))$  is defined for  $1 + \xi(\frac{x-\mu}{\sigma}) > 0$ ; elsewhere,  $\Psi(x)$  is either 176 0 or 1 (Smith (2001)). 177 The stationary form of the GEV has been studied and applied in nu-178 merous studies (Leadbetter et al. (1983); Coles (2001); Schlather (2002); 179 Li et al. (2005); Reiss and Thomas (2007); Papalexiou and Koutsoyian-180 nis (2013)). Under stationarity, the model parameters are time invari-181 ant (Renard et al. (2013)). In practice, many environmental time series 182 vary systematically in response to climatic change, and hence may ex-183 hibit non-stationary behavior (Zwiers and Kharin (1998); Solomon et al. 184 (2007); Rootzén and Katz (2013)). In a non-stationary world, the GEV parameters are time-dependent and thus, the extremal properties of the GEV would vary with time (Meehl et al. (2000); Cheng et al. (2014a)).

In most studies, the non-stationarity is accounted for by assuming the lo-

cation parameter is a linear function of time, while keeping the scale and

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shape parameters constant (Gilleland and Katz (2006); Cooley (2009); Katz (2010); Renard et al. (2013)):

$$\mu(t) = \mu_1 t + \mu_0 \tag{2}$$

where  $(\mu_1, \mu_0)$  are regression parameters and t is the time. Technically, 192 a more complex nonlinear model can also be used for non-stationary anal-193 ysis. However, a non-linear model would be more sensitive to the length of the record, and cannot be justified without an evidence of a nonlinear trend. Furthermore, including a trend in the scale parameter and/or shape parameter is straightforward. However, given a lack of evidence that they have changed substantially in the past across the globe, we 198 have not included them in this paper. Given that the objective of this 199 study is to evaluate return levels of the CMIP5 model simulations with 200 ground-based observations, the most stable form of non-stationary ex-201 treme value analysis is used where the location parameter changes over 202 time. 203

In this study, a Bayesian framework is employed to estimate the GEV parameters. This Bayesian framework integrates the information brought by a prior distribution  $p(\theta)$  and the observation vector  $\overrightarrow{y}$  into the posterior distribution of the GEV parameters. For non-stationary GEV parameter estimation, the Bayes theorem can be written as (Winkler (1973); Renard et al. (2006); Cheng et al., (2014)):

$$p(\theta|\overrightarrow{x}) \propto p(\overrightarrow{x}|\theta)p(\theta) = \prod_{t=1}^{N_t} p(x_t|\theta)p(\theta)$$
 (3)

$$p(\beta|\overrightarrow{x},y) \propto p(\overrightarrow{x}|\beta,y)p(\beta|y)$$

$$p(\overrightarrow{x}|\beta,y) = \prod_{t=1}^{N_t} p(x_t|\beta,y(t)) = \prod_{t=1}^{N_t} p(x_t|\mu(t),\sigma,\xi)$$
(4)

where  $\beta = (\mu_1, \mu_0, \sigma, \xi)$ , and y(t) is the covariate value under non-210 stationarity. The parameters of the GEV distribution including  $\mu_0, \mu_1, \sigma, \xi$ 211 are derived by generating random realizations from the posterior distri-212 butions of the model parameters using the Differential Evolution Markov 213 Chain (DE-MC; ter Braak (2004); Vrugt et al. (2009)). In fact, the DE-214 MC, with a Metropolis-Hastings (Renard et al. (2013)) step to update 215 each parameter, is used to derive a sample from the posterior distribu-216 tions of the GEV model parameters whose initial states are determined by a maximum likelihood method (Coles (2001)). A statistical method 218 known as the criterion  $\widehat{R}$  (Gelman and Shirley (2011)) is adopted for convergence checking. A detailed explanation of the parameter estima-220 tion approach used in this study is provided in Renard et al. (2013). 221 Compared to the conventional Markov Chain Monte Carlo (MCMC) al-222 gorithm, the DE-MC exhibits faster calculation and convergence speed 223 (ter Braak (2006)). In this approach, the parameters are estimated based 224 on the posterior of the MCMC samples for each pixel separately.

The fitted GEV distribution is then used to derive the return levels
of annual temperature maxima of CMIP5 climate simulations and CRU
reference observations. The median of the estimated location parameter,
obtained from the DE-MC procedure, is used as the final location parameter:
eter:

$$\widetilde{\mu}_m = median(\mu(1), \mu(2), ..., \mu(t)) \tag{5}$$

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While here the median of the DE-MC samples is selected form simulations, more conservative quantiles (90th, 95th percentile) can also be used depending on the objective of the study (Cheng et al. (2014a)).

It should be noted that the DE-MC Bayesian approach provides posterior distributions of the model parameters. For this reason, upper and lower bounds (or other quantiles) of uncertainty can be derived using the upper and lower bounds of the parameters' posterior distributions.

In this study, return levels in model simulations and observations are evaluated. The return level is defined as a function of the return period T explained above (Cooley (2013)):

$$T = \frac{1}{1 - p} \tag{6}$$

probability can be obtained using either a non-parametric approach (Makkonen (2006)) or a parametric distribution function such as the GEV. Here, the return levels of temperature extremes are computed for five return periods: T=2, T=10, T=25, T=50, and T=100.

The presence of non-stationarity is tested by means of the commonly used Mann-Kendall trend test (Mann (1945); Kendall (1976)) at the  $\alpha=0.05$  significance level. If the null hypothesis of no trend cannot

be rejected, we assume a stationary climate. The stationary GEV-based

p-return level (p-quantile curve,  $q_p$ ) can be derived as:

where p is the non-exceedance occurrence probability. The non-exceedance

$$q_p = \left( \left( -\frac{1}{\log p} \right)^{\xi} - 1 \right) \times \frac{\sigma}{\xi} + \mu, for \ \xi \neq 0$$
 (7)

If the null hypothesis of no trend is rejected (data exhibits non-stationary behavior), we assume a non-stationary condition with respect to tem-

perature extremes. The non-stationary GEV-based return level is then estimated as:

$$q_p = \left( \left( -\frac{1}{\log \widetilde{p}} \right)^{\xi} - 1 \right) \times \frac{\sigma}{\xi} + \widetilde{\mu}_m, for \ \xi \neq 0$$
 (8)

where  $\widetilde{\mu}_m$  is defined in Equation 5 and  $\widetilde{p}$  is the corresponding proba-255 bility. It should be noted that the Mann-Kendall trend test is only used 256 to avoid implementing a non-stationary model on a time series that does 257 not exhibit a statistically significant change in extremes. However, the methodology is general and can be applied to the data, regardless of the underlying trend. To further evaluate the fit of the non-stationary 260 model, the Bayes Factor (Kass and Raftery (1995)) is implemented to check the null hypothesis of no trend. The Bayes factor evaluates the 262 null-hypothesis of no trend against the alternative using the posterior 263 distributions of sampled parameters (Kass and Raftery (1995)).

#### 4 Results

### 4.1 Representation of Annual Temperature Maxima

In the first step, the annual maxima of CMIP5 temperature simulations,
determined from monthly time series, are compared with those of the
CRU observations. Figure 1 (top left) displays the mean annual temperature maxima from 1901 to 2005 as represented by CRU observations. The
rest of the panels in Figure 1 demonstrate the differences between CMIP5
climate simulations and CRU observations (CMIP5 model - observation).
In this figure, positive (negative) values indicate overestimation (underestimation) of the annual temperature maxima. Figure 1 shows the results
for the 17 CMIP5 models listed in Table 1. One can see that the climate models individually display different patterns of overestimation and

underestimation. The discrepancies between the model simulations and observations are primarily within  $\pm$  1 to 3 °C. However, local errors for some regions may be as high as  $\pm$ 10 °C (see also the empirical cumulative distribution of the mean error in Figure 2).

Figure 1 shows that over the United States most models (except-281 ing HadGEM2-ES\_esm, CCSM4, CSIRO-ACCESS1-0, CESM1-WACCM, 282 MIROC-ESM and CanESM2) tend to underestimate the mean annual 283 temperature maxima by 1 to 3 °C. Here, CanESM2 instead substantially overestimates the mean annual temperature maxima. Over Australia, on the other hand, several models (e.g. CSIRO-ACCESS1-0, HadGEM2-ES\_esm, MPI-ESM-P and CanESM2) demonstrate little or no bias. Over 287 Amazonia, the mean annual temperature maxima are mostly underesti-288 mated, except in a few models (e.g., GFDL-CM3, CanESM2) where they 289 are overestimated. 290

The results indicate that model simulations particularly diverge from 291 one another over cold regions (e.g., northern Russia, and Canada) except for Greenland, where most models (but not MIROC-ESM and IN-293 MCM4\_esm) underestimate the mean annual temperature maxima. Such 294 a consistent underestimation could substantially impact model-based anal-295 vses of changes in ice-sheets, and snow/glacier melt studies. Krabill et al. 296 (2004) reported that Greenland is losing coastal ice sheets quite rapidly 297 (see also Ren et al. (2011); Kjær et al. (2012)). CMIP5 models' underes-298 timation of annual maxima climatology implies that the ice loss rate in 299 Greenland might be greater than that reported in model-based studies. 300 Similar to the modeling results by Alley et al. (2005) and Reeh (1989), 301 rapid ice-marginal changes may indicate greater ice-sheet sensitivity to warming than has been acknowledged previously. However, over other 303 cold regions that are at most risk of accelerated ice melt (e.g. Alaska,

Northern Canada, and Siberia), most models tend to overestimate the mean annual temperature maxima relative to the CRU reference data (Figure 1).

It is also noteworthy that the model simulations collectively under-308 estimate the mean annual maxima over arid and semi-arid regions (e.g., 309 Sahara, southwestern U.S.), that are most subject to severe heat waves. 310 Considering the magnitudes of deviations from the CRU, there is a better 311 agreement between CMIP5 simulations and observations in such subtrop-312 ical regions than in high-latitude cold regions. This is consistent with the 313 findings reported in Kharin et al. (2007) based on CMIP3 climate model 314 simulations. 315

Figure 2 displays the ensemble mean (a), inter-model standard deviation (b), and range (c) of the annual temperature maxima in CMIP5 simulations, as well as the empirical cumulative distribution function (CDF) of the mean error relative to observations (d). The figure shows that the inter-model variability and range of simulations are more variable over Siberia, the western United States, and parts of the Middle East and Sahara compared to other regions.

#### 323 4.2 Return Levels of Temperature Extremes

Using the annual temperature maxima from CMIP5 multi-model simulations and CRU observations, temperature return levels are derived for different return periods by fitting the appropriate type of GEV (stationary/nonstationary) to the block maxima of temperature extremes. Return levels of annual temperature maxima are derived and reported for the return periods T of 2, 10, 25, 50, and 100 years.

As an example, Figure 3 shows the 2-year temperature return levels based on CRU observations (top left) and on the selected subset of 17

CMIP5 climate model simulations. In Figure 3, the global temperature values range from -11 to 35 °C. Overall, Figure 3 indicates that there are good agreements between the observed and CMIP5 simulated *spatial* patterns of 2-year annual temperature maxima, but that the magnitudes of 2-year annual temperature maxima represented by the selected CMIP5 models differ substantially.

Figure 4 presents the differences in CMIP5 simulated 2-year annual 338 temperature maxima with respect to CRU observations. One can see that there are variations in both the magnitude and sign of the error of 2-year return levels across CMIP5 climate simulations. This implies that CMIP5 climate models capture the spatial patterns of temperature extremes well; 342 however, individual models may be biased with respect to observations. 343 As shown, over most parts of the world, the biases are within  $\pm 4$  °C. For a 344 higher return level, one expects the differences in temperature simulations 345 to increase relative to observations. For example, Figure 5 presents the 346 differences in 25-year-return annual temperature maxima, as simulated by 347 CMIP5 models with respect to CRU temperature observations. As shown, the patterns of differences remain similar, but the range of differences between simulated and observed annual temperature maxima increases at 25-year return level relative to the 2-year return level. 351

As another example, Figure 6 displays the 100-year return levels for the CRU observations and the selected CMIP5 simulations. One can see that the patterns of annual temperature maxima are similar to those of Figure 3, but with higher magnitudes of annual temperature maxima (as expected). The figure shows that the warmest months across the globe typically occur over the Sahara, the Middle East, and Australia. The differences in CMIP5 100-year simulated and observed annual temperature maxima are presented in Figure 7. As shown, the biases of the

25-, and 100-year return temperature simulations are larger than those of 2-year-return simulations in Figure 4. However, the spatial patterns of temperature extremes are in a good agreement with CRU observations and consistent across different return periods (compare the model simulations with the upper left panels in Figures 3 and 6). Overall, the regional biases of simulated annual temperature extremes at high return levels (e.g., 100-year) are consistent with those of the lower return levels (e.g., 2-year).

Not shown here for brevity are the spatial patterns and biases of 10-368 , 25- and 50-year return levels of extreme temperature simulations by 369 CMIP5 models, which are consistent with the results presented in Fig-370 ures 3 to 7. For a quantitative evaluation of the extremal simulation by 371 CMIP5 models, Figure 8(top) summarizes the Mean Error (ME) for all 372 the 41 CMIP5 climate model simulations of 2-, 10-, 25-, 50, and 100-year 373 annual temperature maxima return levels with respect to CRU observations. As anticipated, ME values are larger at higher return levels. One can see that considering the global averages, most models overestimate 376 the simulated return levels of the annual temperature maxima, while fewer 377 models (e.g., FGOALS-g2, INMCM4\_esm, NorESM1-ME) underestimate 378 the temperature extremes. Among the models, FGOALS-s2, CanESM2 379 and MIROC5 exhibit the highest global averages of the ME of the an-380 nual temperature maxima. Most models either systematically overesti-381 mate or underestimate the extreme return levels, except the BCC model 382 experiments in which the shorter return levels (2- and 10-year) are un-383 derestimated and the longer ones are overestimated. Figure 8(bottom) displays boxplots of the differences between CMIP5 simulations and CRU observations. The figure shows medians, 25th and 75th percentiles, and 386 whiskers (variability outside respective percentiles) of differences in Celsius degrees. Figure 8(bottom) indicates that while local differences can be large, most differences (between 25th and 75th percentiles) fall within  $\pm 2$  Celsius degrees.

The MCMC component of the DE-MC model used in this study allows the upper and lower bounds and confidence intervals of the tem-392 perature return levels to be derived based on all model parameters. The 393 uncertainty bounds would be different across either models or space (sim-394 ulation grid boxes). As an example, Figure 9 shows sample uncertainty 395 bounds, median, and the 5% and 95% confidence bounds of the annual 396 temperature maxima based on the DE-MC for CRU reference data and 397 over grid boxes in two different locations in Kansas, United States and 398 eastern China under the non-stationary assumption. The figure confirms that the inference uncertainty is larger at higher return levels (e.g., be-400 cause of larger sampling errors). One can see that the uncertainties of the 401 estimated return levels also vary over different regions. It should be noted 402 that this approach provides uncertainties associated with the statistical 403 analysis of extremes, but does not include uncertainties associated with 404 model physics. 405

As mentioned in Methodology Section, the initial assumption of stationarity and non-stationarity by the Mann-Kendal trend test is tested using the Bayes Factor. As an example, for the selected locations in Figure 9, the Bayes Factor results are provided for testing non-stationarity in extremes to make sure the initial assumption from the Mann-Kendal test is reasonable (see Table 2). As shown in Table 2, the method confirms the initial assumption of non-stationarity by the Mann-Kendal trend test.

#### 5 Discussion and Concluding Remarks

The objective of this study is to evaluate to what extent the CMIP5 climate model simulations can represent observed warm monthly temperature extremes under a changing climate. The biases of simulated annual temperature maxima are quantified for the selected CMIP5 models. Furthermore, the 2-, 10-, 25-, 50, and 100-year return levels of the annual temperature maxima from CMIP5 simulations are compared with those derived from CRU observations.

The results show that most, but not all, CMIP5 climate models tend to underestimate the mean annual temperature maxima over the United States and Amazonia. The CMIP5 models particularly disagree with each 423 other over cold regions (e.g., Russia, northern Canada), with the excep-424 tion of Greenland where most climate models underestimate the mean 425 annual temperature maxima. This underestimation of the annual temper-426 ature maxima is likely to affect model-based representations of changes 427 in ice-sheets and snow/glacier melt. In contrast, over Alaska, Northern 428 Canada and Siberia, most CMIP5 simulations overestimate the annual 429 temperature maxima compared to those derived from the CRU reference data. 431

Over arid and semi-arid regions (e.g., the Sahara, southwestern U.S., and Middle East), most climate models also underestimate the mean annual temperature maxima. Considering the magnitudes of deviations from the CRU, however, there is a better agreement between CMIP5 model simulations and observations in subtropical regions than in high-latitude cold regions.

The return level analyses show that there are good agreements between the observed and CMIP5 simulated spatial patterns of 2-, 10-, 25-, 50and 100-year annual temperature maxima. While the simulated spatial patterns of the temperature extremes are similar, the magnitudes of the return levels of the annual temperature maxima represented by CMIP5 climate models are biased with respect to CRU observations. In addition, there are variations in both the magnitude and sign of the biases of the annual temperature maxima return levels across the CMIP5 simulations. The results reveal that most CMIP5 simulations overestimate the global averages of the annual temperature maxima at different return periods (see Figure 8).

Given the state of the science in climate modeling, one would not ex-449 pect the coupled Atmosphere/Ocean General Circulation Model (AOGCMs) 450 and earth system models (ESMs) to reproduce the magnitudes of the ob-451 served historical extremes very accurately. Rather, one expects the models 452 to reasonably simulate large-scale patterns of change in occurrences of cli-453 mate extremes (Tebaldi et al. (2006)). Overall, the results of this study indicate that the models capture the spatial patterns of temperature ex-455 tremes well, but that individual models are biased relative to the CRU 456 observations. 457

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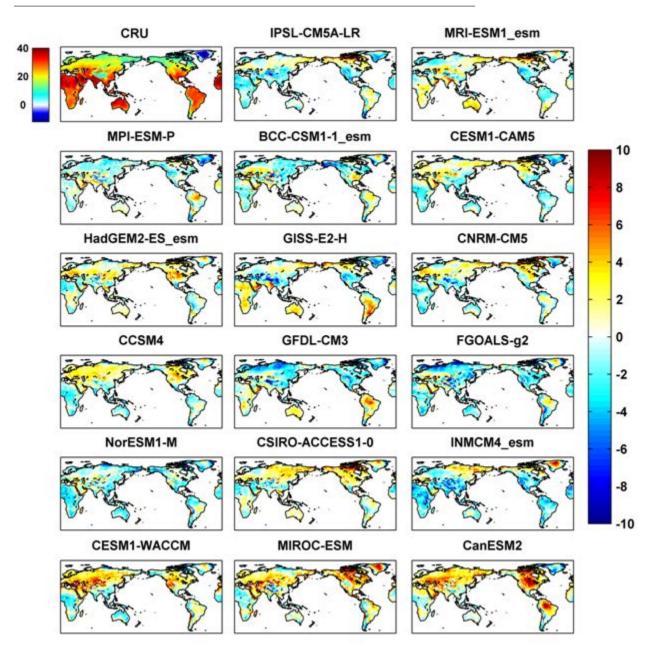
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 $\begin{array}{ll} \textbf{Fig. 1} & \text{Mean annual temperature maxima (in degrees Celsius) based on 1901-2005 Climatic Research Unit (CRU) observations (upper left panel), and the differences between selected CMIP5 climate simulations and CRU reference data (remaining panels).} \end{array}$ 

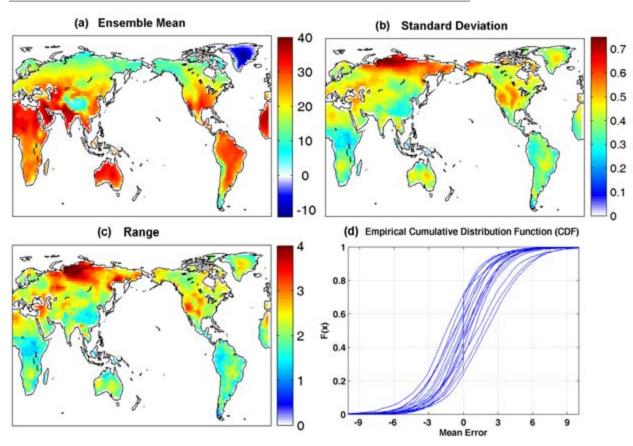
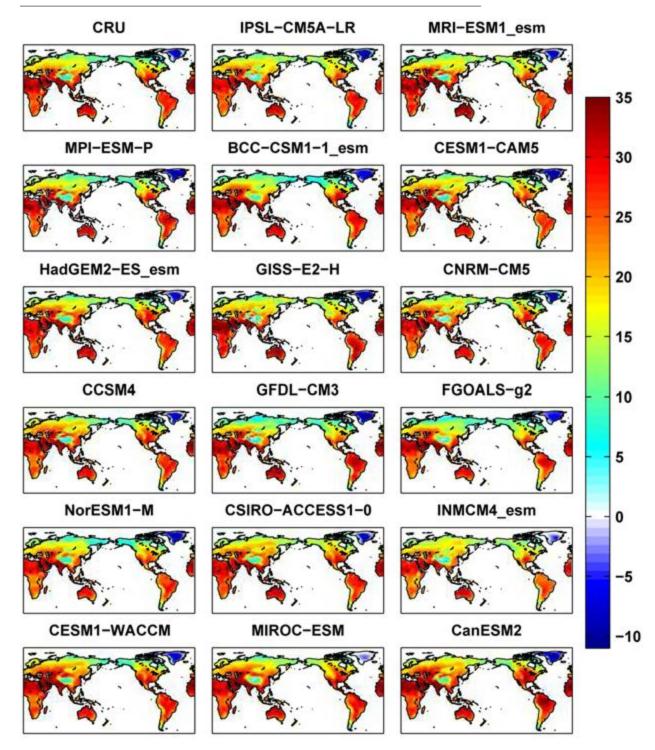
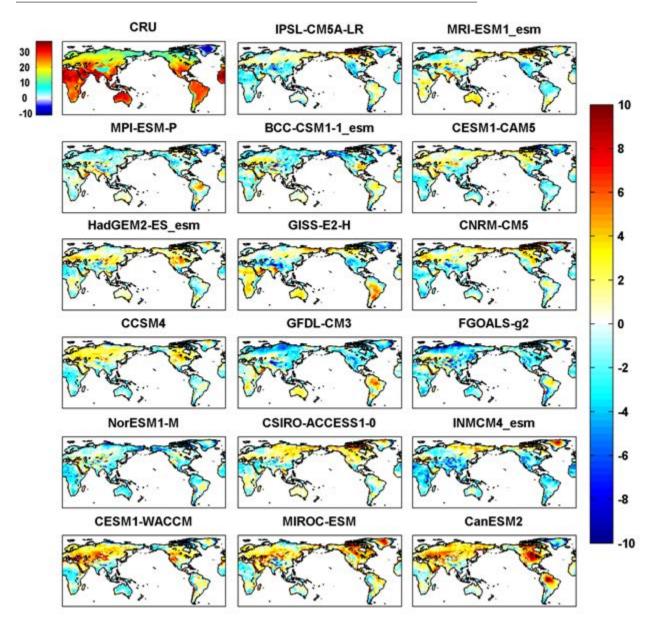


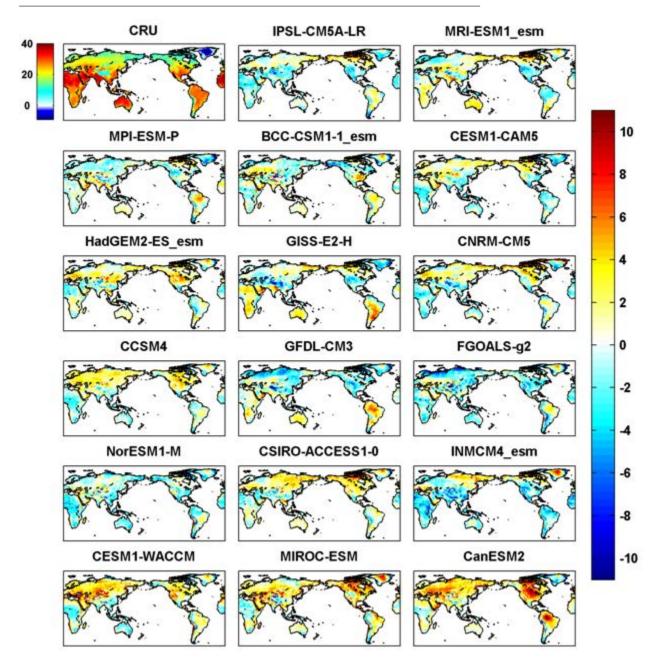
Fig. 2 (a) Ensemble mean, (b) inter-model standard deviation, and (c) range of the annual temperature maxima in CMIP5 simulations. Panel (d) shows the empirical cumulative distribution (CDF) of the mean error of simulations relative to observations.



 $\begin{tabular}{ll} Fig. 3 & 2-year return level (in degrees C) of the annual temperature maxima based on the CRU observations (upper left panel), and on selected CMIP5 climate model simulations (remaining panels). \\ \end{tabular}$ 



 $\begin{tabular}{ll} {\bf Fig.~4~2-year~return~level~(in~degrees~C)~of~the~annual~temperature~maxima~based~on~the~CRU~observations~(upper~left~panel),~and~return-level~differences~between~selected~CMIP5~climate~simulations~and~CRU~reference~data~(CMIP5~-CRU;~remaining~panels). } \label{table_control_c$ 



**Fig. 5** 25-year return level (in degrees C) of the annual temperature maxima from CRU observations (upper left panel), and return-level differences between selected CMIP5 climate simulations and CRU reference data (CMIP5 - CRU; remaining panels).

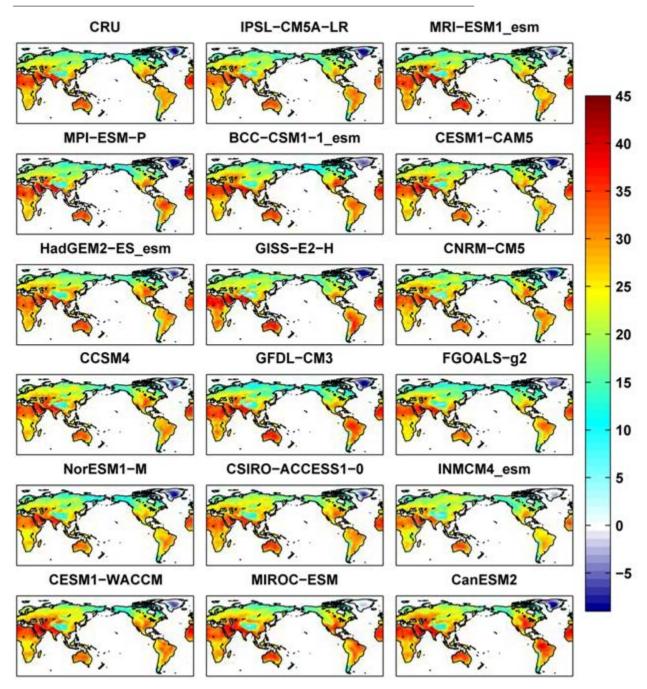
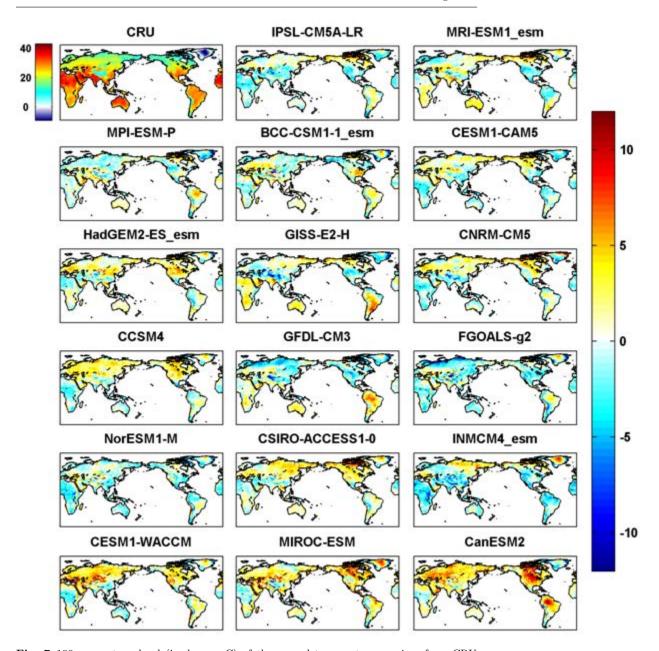


Fig. 6 100-year return level (in degrees C) of the annual temperature maxima based on the CRU observations (upper left panel), and on selected CMIP5 climate model simulations (remaining panels).



**Fig. 7** 100-year return level (in degrees C) of the annual temperature maxima from CRU observations (upper left panel), and return level differences between selected CMIP5 climate simulations and CRU reference data (CMIP5 - CRU; remaining panels).

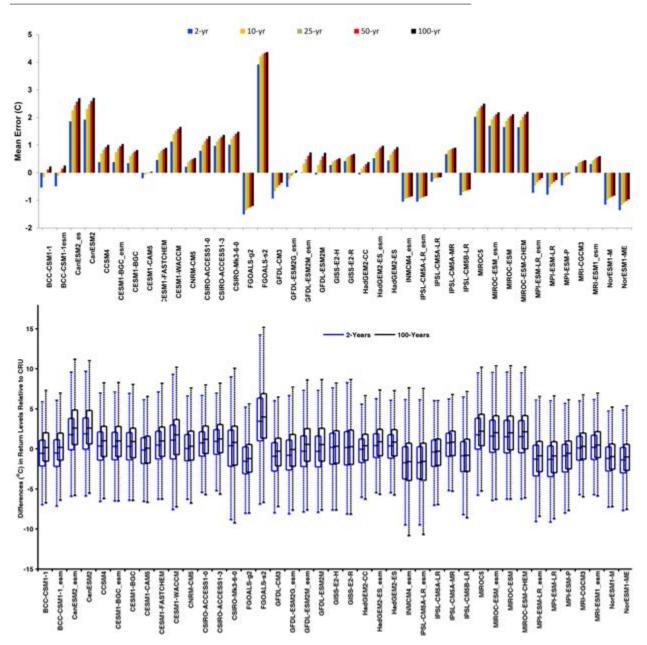


Fig. 8 (top): Mean Error (ME) of the 2-, 10-, 25-, 50-, and 100-year temperature maxima (Degree Celsius) simulations based on 41 CMIP5 simulations relative to Climatic Research Unit (CRU) observations; (bottom): boxplots of differences (degrees C) between CMIP5 2and 100-year return levels relative to CRU observations.

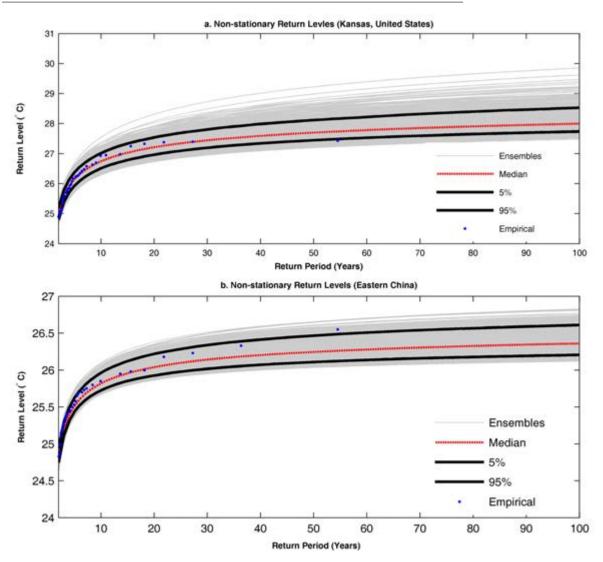


Fig. 9 Sample uncertainty bounds, median, and the 5% and 95% confidence bounds of the annual temperature maxima based on the DE-MC model for CRU reference and over two pixels in a. Kansas, United States and b. eastern China.

 $\begin{tabular}{ll} \textbf{Table 1} List of 17 climate models/experiments whose simulations are displayed in Figures 1 to 7 and their related institutions and countries. The suffix "_esm" designates an historical climate run of an ESM with prescribed emissions $ (1.5) = ($ 

Model/Experiment	Institution	Country	
BCC-CSM1-1_esm	Beijing Climate Center, China Meteorological Administration Cl		
MIROC-ESM	Japan Agency for Marine-Earth Science and Technology,	Japan	
	Atmosphere and Ocean Research Institute,		
	The University of Tokyo		
	National Institute for Environmental Studies		
NorESM1-M	Norwegian Climate Centre Norway		
IPSL-CM5A-LR	Institut Pierre-Simon Laplace France		
GFDL-CM3	NOAA Geophysical Fluid Dynamics Laboratory US.		
CCSM4	National Center for Atmospheric Research US		
GISS-E2-H	NASA Goddard Institute for Space Studies	USA	
$INMCM4\_esm$	Institute for Numerical Mathematics	Russia	
$HadGEM2-ES_{esm}$	Met Office Hadley Centre	UK	
CSIRO-ACCESS1-0	Commonwealth Scientific and Industrial	Australia	
	Research Organisation,		
	and Bureau of Meteorology		
$MRI-ESM1\_esm$	Meteorological Research Institute		
MPI-ESM-P	Max Planck Institute for Meteorology Germa		
CanESM2	Canadian Centre for Climate Modelling and Analysis Ca		
FGOALS-g2	Institute of Atmospheric Physics		
	Chinese Academy of Sciences and Tsinghua University		
CESM1-CAM5	National Science Foundation, Department of Energy,	USA	
	and National Center for Atmospheric Research		
CNRM-CM5	Centre National de Recherches Meteorologiques	France	
	Centre Europeen de Recherche et Formation Avancees		
	en Calcul Scientifique		
CESM1-WACCM	National Science Foundation, Department of Energy,	USA	
	and National Center for Atmospheric Research		

**Table 2** Results of the Bayes Factor at the selected pixels in the Central U.S. and Eastern China. Bayes Factor (K) larger than one indicates the stationary assumption (i.e., null hypothesis) is representative, whereas K < 1 rejects the null hypothesis.

Bayes Factor				
Location	K	Test Interpretation		
Kansas, USA	0.49	Reject Stationary Model		
Eastern China	0.003	Reject Stationary Model		